Name:

BLM 3-3

Section 3.1 Extra Practice

- **1.** For each polynomial function, state the degree. If the function is not a polynomial, explain why.
 - **a)** $h(x) = 5 \frac{1}{x}$

b)
$$y = 4x^2 - 3x + 8$$

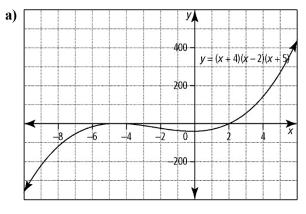
c)
$$g(x) = -9x^{6}$$

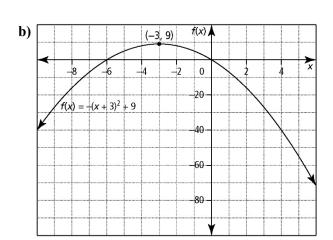
- **d)** $f(x) = \sqrt[3]{x}$
- **2.** What is the leading coefficient and constant term of each polynomial function?

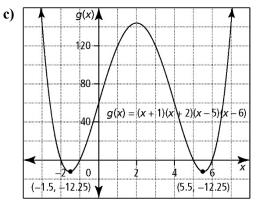
a)
$$f(x) = -x^3 + 2x + 3$$

b) $y = 5 + 9x^4$
c) $g(x) = 3x^4 + 3x^2 - 2x + 1$
d) $k(x) = 9 - 3x - 2x^2$

- **3.** State whether the polynomial function is odd or even. Then, state whether the function has a maximum value, a minimum value, or neither.
 - a) $g(x) = -x^3 + 8x^2 + 7x 1$ b) $f(x) = x^4 + x^2 - x + 10$ c) $p(x) = -2x^5 + 5x^3 - 11x$ d) $h(x) = -3x^2 - 6x - 2$
- **4.** State the number of real *x*-intercepts, domain, and range for each polynomial function.







d)
$$-2x^2(x+3)(x+5)(x-7)$$

5. State the possible number of *x*-intercepts and the value of the *y*-intercept for each polynomial function.

a)
$$f(x) = -x^3 + 2x + 3$$

b) $x = 5 + 0x^4$

b)
$$y = 5 + 9x^{2}$$

- c) $g(x) = 3x^4 + 3x^2 2x + 1$
- **d)** $k(x) = -3x 2x^2$



- **6.** Identify the following characteristics for each polynomial function:
 - the type of function and whether it is of even or odd degree
 - the end behaviour of the graph of the function
 - the number of possible *x*-intercepts
 - whether the function will have a maximum or minimum value
 - the *y*-intercept

a)
$$g(x) = -x^4 + 2x^2 + 7x - 5$$

b)
$$f(x) = 2x^5 + 7x^3 + 12$$

7. Given the polynomial

 $y = -2(x + 1)^{2}(x - 2)(x - 3)^{2}$, determine the following without graphing.

- a) Describe the end behaviour of the graph of the function.
- **b)** Determine the possible number of *x*-intercepts of the function.
- c) Determine the *y*-intercept of the function.
- **d)** Now, use graphing technology to create a sketch of the graph.

- **8.** Identify each function as quadratic, cubic, quartic, or quintic.
 - a) $y = -x^4 + 2x^2 + 7x 5$ b) $f(x) = 2x^5 + 7x^3 + 12$ c) $g(x) = -x^3 + 2x + 3$ d) $k(x) = 9 - 3x - 2x^2$
- 9. The height, *h*, in metres, above the ground of an object dropped from a height of 60 m is related to the length of time, *t*, in seconds, that the object has been falling. The formula is $h = -4.9t^2 + 60$.
 - a) What is the degree of this function?
 - **b)** What are the leading coefficient and constant of this function? What does the constant represent?
 - c) What are the restrictions on the domain of the function? Explain why you selected those restrictions.
 - **d)** Describe the end behaviour of the graph of this function.
- **10.** Using the formula in #9, determine how long an object will take to hit the ground if it is dropped from a height of 60 m. Write your answer to the nearest tenth of a second.



Name: _____ Date: _____

BLM 3-4

Section 3.2 Extra Practice

1. Use long division to divide

 $x^2 - x - 15$ by x - 4.

a) Express the result in the form

$$\frac{P(x)}{x-a} = Q(x) + \frac{R}{x-a} \,.$$

- **b**) Identify any restrictions on the variable.
- c) Write the corresponding statement that can be used to check the division.
- d) Verify your answer.
- 2. Divide the polynomial

$$P(x) = x^4 - 3x^3 + 2x^2 + 55x - 11 \text{ by } x + 3$$

- **a)** Express the result in the form $\frac{P(x)}{x-a} = Q(x) + \frac{R}{x-a}$.
- b) Identify any restrictions on the variable.
- c) Verify your answer.
- 3. Determine each quotient using long division.

a)
$$(3x^2 - 13x - 2) \div (x - 4)$$

b) $\frac{2x^3 - 10x^2 - 15x - 20}{x + 5}$
c) $(2w^4 + 3w^3 - 5w^2 + 2w - 27) \div (w + 3)$

4. Determine each remainder using long division.

a)
$$(3w^3 - 5w^2 + 2w - 27) \div (w - 5)$$

b) $\frac{2x^3 - 8x^2 - 5x - 2}{x + 1}$
c) $(3x^2 - 13x - 2) \div (x + 2)$

5. Determine each quotient using synthetic division.

a)
$$(4w^4 + 3w^3 - 7w^2 + 2w - 1) \div (w + 2)$$

b) $\frac{x^4 + 2x^3 - 8x^2 - 5x - 2}{x - 2}$
c) $(5y^4 + 2y^2 - y + 4) \div (y + 1)$

- 6. Determine each remainder using synthetic division.
 - a) $(3x^2 16x + 5) \div (x 5)$ b) $(2x^4 - 3x^3 - 5x^2 + 6x - 1) \div (x + 3)$ c) $(4x^3 + 5x^2 - 7) \div (x - 2)$
- 7. Use the remainder theorem to determine the remainder when each polynomial is divided by x + 2. a) $-4x^4 - 3x^3 + 2x^2 - x + 5$ b) $7x^5 + 5x^4 + 23x^2 + 8$ c) $8x^3 - 1$
- 8. Determine the remainder resulting from each division.
 - a) $(3x^3 4x^2 + 6x 9) \div (x + 1)$ b) $(3x^2 - 8x + 4) \div (x - 2)$ c) $(6x^3 - 5x^2 - 7x + 9) \div (x + 5)$
- 9. For $(2x^3 + 5x^2 kx + 9) \div (x + 3)$, determine the value of k if the remainder is 6.
- 10. When $4x^2 8x 20$ is divided by x + k, the remainder is 12. Determine the value(s) of k.