Gr 12 9.1 Solutions

1. a) B b) C c) $\mathrm{D} \quad$ d) A


| Characteristic | $y=\frac{5}{x-2}$ |
| :---: | :---: |
| Non-permissible value | $x=2$ |
| Behaviour near nonpermissible value | As $x$ approaches $2,\|y\|$ becomes very large. |
| End behaviour | As $\|x\|$ becomes very large, $y$ approaches 0 . |
| Domain | $\{x \mid x \neq 2, x \in \mathrm{R}\}$ |
| Range | $\{y \mid y \neq 0, y \in \mathrm{R}\}$ |
| Equation of vertical asymptote | $x=2$ |
| Equation of horizontal asymptote | $y=0$ |

3. a)

domain: $\{x \mid x \neq 1, x \in \mathrm{R}\}$; range: $\{y \mid y \neq 0, y \in \mathrm{R}\}$; intercept: $(0,-3)$; asymptotes: $x=1, y=0$
b)

domain: $\{x \mid x \neq 0, x \in \mathrm{R}\}$; range: $\{y \mid y \neq 6, y \in \mathrm{R}\}$; intercept: $\left(-\frac{1}{3}, 0\right)$; asymptotes: $x=0, y=6$
c)

domain: $\{x \mid x \neq-4, x \in \mathrm{R}\} ;$ range: $\{y \mid y \neq-2, y \in \mathrm{R}\}$;
intercepts: $(0,-0.75),(-1.5,0)$; asymptotes: $x=-4, y=-2$
d)

domain: $\{x \mid x \neq-2, x \in \mathrm{R}\}$; range: $\{y \mid y \neq 8, y \in \mathrm{R}\}$; intercepts: $(0,8.5),(-2.125,0)$; asymptotes: $x=-2, y=8$
4. a)

asymptotes: $x=1, y=2$;
intercepts: $(-2.5,0),(0,-5)$
b)

asymptotes: $x=-2, y=4$;
intercepts: $(0,-1.5),(0.75,0)$
5. a) $y=\frac{3}{x}$
b) $y=\frac{4}{x}$
c) $y=\frac{2}{x-5}$
d) $y=-\frac{2}{x+4}$
6. a) $a=3, k=4$
b)

7. 



The graph of $y=\frac{1}{x^{2}+6 x+9}$ is the graph of $y=\frac{1}{x^{2}}$
translated 3 units left.
8.

| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :---: | :---: |
| -5 | 0.92 |
| -2 | 0.56 |
| 1 | -0.17 |
| 4 | -2.33 |
| 7 | undefined |
| 10 | 6.33 |
| 13 | 4.17 |
| 16 | 3.44 |
| 19 | 3.08 |



| Characteristic | $\boldsymbol{y}=\frac{\mathbf{2 x - 1}}{\boldsymbol{x}-\mathbf{7}}$ |
| :--- | :---: |
| Non-permissible value | $x=7$ |
| Behaviour near non- <br> permissible value | As $x$ approaches $7,\|y\|$ <br> becomes very large. |
| End behaviour | As $\|x\|$ becomes very <br> large, $y$ approaches 2. |
| Domain | $\{x \mid x \neq 7, x \in \mathrm{R}\}$ |
| Range | $\{y \mid y \neq 2, y \in \mathrm{R}\}$ |
| Equation of vertical <br> asymptote | $y=7$ |
| Equation of horizontal <br> asymptote |  |

9. a) $t=\frac{d}{s}$
b) $t=\frac{351}{65}=5.4$, so 5.4 hours or 5 h and 24 min
c) $70.2 \mathrm{~km} / \mathrm{h}$

BLM 9-3 Section 9.2 Extra Practice

1. point of discontinuity at $\left(-3, \frac{1}{10}\right)$ vertical asymptote: $x=7$
2. You can factor the denominator: $y=\frac{x+2}{(x+2)(x+1)}$.

Since the factor $(x+2)$ appears in the numerator and denominator, the graph will have a point of discontinuity at $(-2,-1)$. The factor $(x+1)$ appears in the denominator only, so there will be an asymptote at $x=-1$.
3.

| Characteristic | $\boldsymbol{y}=\frac{(x+3)(\boldsymbol{x}-\mathbf{2})}{(\boldsymbol{x}+\mathbf{5})(\boldsymbol{x}+\mathbf{3})}$ |
| :--- | :--- |
| Non-permissible <br> value(s) | $x=-5$ and $x=-3$ |
| Feature exhibited at <br> each non-permissible <br> value | asymptote at $x=-5 ;$ <br> point of discontinuity at <br> $(-3,-2.5)$ |
| Behaviour near each <br> non-permissible value | As $x$ approaches $-5,\|y\|$ <br> becomes very large. <br> As $x$ approaches $-3, y$ <br> approaches -2.5. |
| Domain | $\{x \mid x \neq-3,-5, x \in \mathrm{R}\}$ |
| Range | $\left\{y \mid y \neq 1,-\frac{5}{2}, y \in \mathrm{R}\right\}$ |

4. a)

| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :--- | :--- |
| -0.9 | 3.1 |
| -0.99 | 3.01 |
| -0.999 | 3.001 |
| -0.9999 | 3.0001 |
| -1 | undefined |
| -1.0001 | 2.9999 |
| -1.001 | 2.999 |
| -1.01 | 2.99 |
| -1.1 | 2.9 |

As $x$ approaches $-1, y$ approaches 3 .
b)

| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :--- | :---: |
| 1.9 | -4.23809524 |
| 1.99 | -4.47263682 |
| 1.999 | -4.49725137 |
| 1.9999 | -4.49972501 |
| 2 | undefined |
| 2.0001 | -4.50027501 |
| 2.001 | -4.50275138 |
| 2.01 | -4.52763819 |
| 2.1 | -4.78947368 |


| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :--- | ---: |
| 3.9 | -109 |
| 3.99 | -1099 |


| 3.999 | -10999 |
| :--- | ---: |
| 3.9999 | -109999 |
| 4 | undefined |
| 4.0001 | 110001 |
| 4.001 | 11001 |
| 4.01 | 1101 |
| 4.1 | 111 |

As $x$ approaches 2, $y$ approaches -4.5 , and as $x$ approaches $4,|y|$ becomes very large, approaching negative infinity or positive infinity.
5. a) vertical asymptote: $x=-2$; point of discontinuity at $\left(-5, \frac{5}{3}\right)$;
$x$-intercept: $(0,0) ; y$-intercept: $(0,0)$

b) vertical asymptote: $x=-3$; point of discontinuity at $\left(3,-\frac{1}{16}\right)$;
$x$-intercept: $(4,0) ; y$-intercept: $\left(0,-\frac{4}{3}\right)$

c) no vertical asymptote; point of discontinuity at $(-1,3)$; $x$-intercept: $(-4,0) ; y$-intercept: $(0,4)$

d) no vertical asymptote; point of discontinuity at $(-3,-7)$; $x$-intercept: $(0.5,0) ; y$-intercept: $(0,-1)$

6.

| Characteristic | $\boldsymbol{y}=\frac{\boldsymbol{x}^{2}-\mathbf{3 x}}{\mathbf{3 x - 9}}$ | $\boldsymbol{y}=\frac{\boldsymbol{x}^{\mathbf{2}}+\mathbf{3 x}}{\mathbf{3 x - 9}}$ |
| :--- | :--- | :--- |
| Non- <br> permissible <br> value(s) | $x=3$ | $x=3$ |
| Feature <br> exhibited at <br> each non- <br> permissible <br> value | point of <br> discontinuity | asymptote |
| Behaviour near <br> each non- <br> permissible <br> value | As $x$ <br> approaches 3, <br> $y$ approaches <br> 1. | As $x$ <br> approaches 3, <br> ly\| becomes <br> very large. |

7. a) C; Example: In factored form, the rational function has two non-permissible values in the denominator, which do not appear in the numerator. Therefore, the graph with two asymptotes is the most appropriate choice.
b) B; Example: In factored form, the rational function has one non-permissible value that appears in both the numerator and denominator, and another nonpermissible value that is only in the denominator. Therefore, the graph with one asymptote and one point of discontinuity is the most appropriate choice. c) A; Example: In factored form, one non-permissible value appears in the numerator and denominator. Therefore, the graph has a point of discontinuity, but no asymptote.
8. a) $y=\frac{(x-3)(x+2)}{(x-3)}$ or $y=\frac{x^{2}-x-6}{x-3}$
b) $y=\frac{(x-2)(x+2)}{(x+2)}$ or $y=\frac{x^{2}-4}{x+2}$
c) $y=\frac{(x+4)}{(4-x)(4+x)}$ or $y=\frac{x+4}{16-x^{2}}$
d) $y=\frac{(x+5)}{(x+3)(x+5)}$ or $y=\frac{x+5}{x^{2}+8 x+15}$
9. Example: $y=\frac{-12(2 x+5)}{(x-2)(2 x+5)}$

BLM 9-4 Section 9.3 Extra Practice
$\begin{array}{llll}\text { 1. a) } x=\frac{3}{5} & \text { b) } x=5 & \text { c) } x=24 & \text { d) } x=4\end{array}$
$\begin{array}{ll}\text { 2. a) } x=10 \text { and } x=-4 & \text { b) } x=7 \text { and } x=1\end{array}$
c) $x=10$ and $x=-3$
d) $x=\frac{3}{2}$ and $x=-2$
3. a) $x=5$ and $x=1$
b)

c) The value of the function is 0 when the value of $x$ is 1 or 5 . The $x$-intercepts of the graph of the function are the same as the roots of the corresponding equation.
4. a) $x=0$ and $x=3.5$

b) $x=-2$ and $x=6$

c) $x=-0.25$ and $x=-2$

5. a) $0=x^{2}-8 x+12$

$x=2$ and $x=6$
b) $y=\frac{6-2 x}{x^{2}-1}$

$x=3$
6. a) $x \approx 0.76$ and $x \approx 5.24$ b) $x \approx-2.79$ and $x \approx 1.79$
c) $x \approx 0.53$ and $x \approx 4.87$
7. a)

$x \approx 0.63$
b)

$x \approx 0.85$ and $x \approx 6.15$
8. The solution $n=3$ is a non-permissible value, so there is no solution.
9. Carmen: 36 h; James: 45 h

