## Gr 11 Ch 3 Answers:

## BLM 3-2 Chapter 3 Prerequisite Skills

1. a) $8 x^{2}-4 x$ b) $4 x^{2}+25 x-21$
c) $4 x^{2}-20 x+25$ d) $-x^{2}+3 x+13$
2. a) -3 b) $m=\frac{3}{2}$ c) $y=\frac{3}{2} x-3$
d) all real numbers or $\{y \mid y \in \mathrm{R}\}$ e) 2
3. Example: $(14,-1.2),(19,-3.2)$
4. a) $3 x+4 y-8=0$ b) $2 x+y+2=0$
5. a) $y=-3 x+4 ; m=-3 ; y$-intercept $=4$
b) $y=\frac{3}{7} x-\frac{1}{7} ; m=\frac{3}{7} ; y$-intercept $=-\frac{1}{7}$
c) $y=\frac{3}{4} x ; m=\frac{3}{4} ; y$-intercept $=0$
6. a) $5 x+y-2=0 ; A=5, B=1, C=-2$
b) $-2 x+3 y+21=0 ; A=-2, B=3, C=21$
c) $3 x-16 y-4=0$; $A=3, B=-16, C=-4$
7. a) Label the horizontal axis $x$ and the vertical axis $g(x)$. b) -14
c) Yes. If you substitute $x=5$, you get $g(5)=7$.
d) $g$ is the set of all real numbers
8. a) 9 b) $\frac{81}{4}$ c) $\frac{49}{16}$
9. a) 1 b) 3 c) 2
10. a) The $y$-intercept could have a value of -1 .

| $\boldsymbol{x}$ | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | -4 | -1 | 2 | 5 | 8 |


b) The $y$-intercept could have a value of 2 .

| $\boldsymbol{x}$ | -3 | 0 | 3 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 0 | 2 | 4 | 6 | $\frac{20}{3}$ |


11. a)

b) $p(50)=37 ; p(150)=31 ; p(200)=28$
c) $\{p(x) \mid 28 \leq p(x) \leq 37\}$

## BLM 3-4 Section 3.1 Extra Practice

1. a) The graph can be obtained by applying a change in width about the $x$-axis by a factor of 3 . The graph opens upward, has a minimum $y$-value of 0 , and the range is $y \geq 0$.
b) The graph can be obtained by applying a change in width about the $x$-axis by a factor of 5 , and then a reflection in the $x$-axis. The graph opens downward, has a maximum $y$-value of 0 , and the range is $y \leq 0$. c) The graph can be obtained by applying a vertical translation up 8 units. The graph opens upward, has a minimum $y$-value of 8 , and the range is $y \geq 8$.
d) The graph can be obtained by applying a vertical translation down 5 units. The graph opens upward, has a minimum $y$-value of -5 , and the range is $y \geq-5$. 2. a) The graph of $y=(x-6)^{2}$ can be obtained from $y=x^{2}$ by applying a horizontal translation 6 units to the right.

vertex: $(6,0)$; axis of symmetry: $x=6$;
domain: $x \in R$; range: $y \geq 0 ; x$-intercept: $x=6$; $y$-intercept: $y=36$
b) The graph of $y=(x+1)^{2}$ can be obtained by applying a horizontal translation 1 unit to the left.

vertex: $(-1,0)$; axis of symmetry: $x=-1$; domain: $x \in \mathrm{R}$; range: $y \geq 0$; $x$-intercept: $x=-1$; $y$-intercept: $y=1$
c) The graph of $y=(x+4)^{2}+3$ can be obtained by applying a horizontal translation 4 units to the left and a vertical translation 3 units up.

vertex: $(-4,3)$; axis of symmetry: $x=-4$; domain: $x \in \mathrm{R}$; range: $y \geq 3$; $x$-intercept: none; $y$-intercept: $y=19$
d) The graph of $y=(x-2)^{2}-1$ can be obtained by applying a horizontal translation 2 units to the right and a vertical translation 1 unit down.

vertex: $(2,-1)$; axis of symmetry: $x=2$;
domain: $x \in \mathrm{R}$; range: $y \geq-1$; $x$-intercepts: $x=1$ and 3; $y$-intercept: $y=3$
2. a) $y=0.5 x^{2}$
b) $y=-0.5 x^{2}$
c) $y=0.5(x+6)^{2}$
d) $y=0.5 x^{2}-3$
3. a) The graph can be obtained from the graph of $f(x)=x^{2}$ by applying a horizontal translation 7 units to the left, and a vertical translation 3 units down.
b) The graph can be obtained from the graph of $f(x)=x^{2}$ by applying a change in width about the $x$-axis by a factor of 2 , a reflection in the $x$-axis, and a vertical translation 5 units up.
c) The graph can be obtained from the graph of $f(x)=x^{2}$ by applying a change in width about the $x$-axis by a factor of $\frac{1}{3}$, a reflection in the $x$-axis, and a horizontal translation 3 units to the right.
d) The graph can be obtained from the graph of $f(x)=x^{2}$ by applying a change in width about the $x$-axis by a factor of 4 , a horizontal translation 2 units to the left, and a vertical translation 1 unit down.
4. 

|  | a) | b) | c) | d) |
| :--- | :---: | :---: | :---: | :---: |
| Vertex | $(5,1)$ | $(-2,0)$ | $(-4,-5)$ | $(0,3)$ |
| Axis of <br> symmetry | $x=5$ | $x=-2$ | $x=-4$ | $x=0$ |
| Direction | upward | downward | upward | downward |
| Max/min | $\min y=1$ | $\max y=0$ | $\min y=-5$ | $\max y=3$ |
| Domain | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ |
| Range | $y \geq 1$ | $y \leq 0$ | $y \geq-5$ | $y \leq 3$ |
| Number of <br> $x$-intercepts | 0 | 1 | 2 | 2 |

6. a) $y=3(x-2)^{2}$ b) $y=-2(x+2)^{2}+3$
c) $y=\frac{1}{2}(x-3)^{2}-2$ d) $y=-1(x-4)^{2}+1$
7. a) $f(x)=-2(x-5)^{2}$ b) $f(x)=\frac{2}{3}(x-2)^{2}-6$

## BLM 3-5 Section 3.2 Extra Practice

1. a) Yes. The function fits the standard form of a quadratic function with $a=1, b=-15$, and $c=0$. b) $y=x^{2}-16$ Yes. The function fits the standard form of a quadratic function with $a=1, b=0$, and $c=-16$.
c) Yes. The function fits the standard form of a quadratic function with $a=-4.9, b=0$, and $c=400$.
d) No. The function does not fit the standard form of a quadratic function.
2. |  | a) | b) |
| :--- | :---: | :---: |
| Vertex | $(-1,-4)$ | $(-1,9)$ |
| Axis of symmetry | $x=-1$ | $x=-1$ |
| $\boldsymbol{x}$-intercepts | -3 and 1 | -4 and 2 |
| $\boldsymbol{y}$-intercept | -3 | 8 |
| Direction | upward | downward |

| Max/min | $\min y=-4$ | $\max y=9$ |
| :--- | :---: | :---: |
| Domain | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ |
| Range | $y \geq-4$ | $y \leq 9$ |

3. a) $y=x^{2}+14 x+39$ b) $f(x)=-6 x^{2}-3 x+30$
c) $h(t)=-9 t^{2}-18 t+41$ d) $y=8 x^{2}+26 x+15$

4. a)
b)

c)

d)


|  | a) | b) | c) | d) |
| :--- | :---: | :---: | :---: | :---: |
| Vertex | $(4,-1)$ | $(-4,9)$ | $(2,-4)$ | $(1,5)$ |
| Axis of <br> symmetry | $x=4$ | $x=-4$ | $x=2$ | $t=1$ |
| $\boldsymbol{x}$-intercepts | 3 and 5 | -1 and -7 | 0 and 4 | 0 and 2 |
| $\boldsymbol{y}$-intercept | 15 | -7 | 0 | 0 |
| Direction | upward | downward | upward | downward |
| Max/min | min: -1 | max: 9 | $\min :-4$ | max: 5 |
| Domain | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ | $t \in \mathrm{R}$ |
| Range | $y \geq-1$ | $f(x) \leq 9$ | $y \geq-4$ | $h(t) \leq 5$ |

5. a) $w=$ width; 2 width + length $=200 \mathrm{~m}$ of fencing, so length $=200-2 w$
b) $A(w)=w(200-2 w)$ or $A(w)=-2 w^{2}+200 w$

d) $5000 \mathrm{~m}^{2}$ e) 50 m by 100 m

b) 100 m ; this represents the initial height of the projectile
c) 21.9 s ; this represents the time that the projectile is in the air
d) 651.25 m ; occurs at 10.5 s

## BLM 3-6 Section 3.3 Extra Practice

1. a) 25 ; $(x-5)^{2}$ b) $16 ;(x+4)^{2}$ c) $36 ;(x-6)^{2}$
d) 1 ; $(x+1)^{2}$
2. a) $y=(x+1)^{2}-5 ;(-1,-5)$
b) $y=(x-3)^{2}+4 ;(3,4)$
c) $y=(x+4)^{2}-10 ;(-4,-10)$
d) $y=(x+12)^{2}-90 ;(-12,-90)$
3. a) $y=3(x-2)^{2}+1$ b) $y=-2(x+5)^{2}-6$
c) $y=6(x-4)^{2}-96$ d) $y=-4(x+7)^{2}$
4. a) $y=(x+3)^{2}-5$; min of -5 when $x=-3$

b) $y=2(x-4)^{2}-1$; min of -1 when $x=4$

c) $y=-3(x+2)^{2}+5$; max of 5 when $x=-2$

d) $y=-1(x-9)^{2}+81$; max of 81 when $x=9$

5. 

|  | a) | b) | c) | d) |
| :--- | :---: | :---: | :---: | :---: |
| Vertex | $(-5,-9)$ | $(-1,6)$ | $(-7.5,4.5)$ | $\left(\frac{1}{3}, \frac{2}{3}\right)$ |
| Axis of <br> symmetry | $x=-5$ | $x=-1$ | $x=-7.5$ | $x=\frac{1}{3}$ |
| Max/min | $\min y=-9$ | $\max y=6$ | $\min y=4.5$ | $\min y=\frac{2}{3}$ |
| Domain | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ | $x \in \mathrm{R}$ |
| Range | $y \geq-9$ | $y \leq 6$ | $y \geq 4.5$ | $y \geq \frac{2}{3}$ |

6. a) $R(x)=(1200+100 x)(6.00-0.30 x)$
b) 4 weeks; $\$ 7680$
c) Example: Assume that yield increases will remain constant at 100 bushels per week; assume price will decrease at $30 \notin$ each week.
