4.4 Introduction to Trigonometric Equations

To solve trigonometric equations, isolate the trigonometric ratio and solve using the techniques from chapter 4.3.

Example 1:

Solve in the specified domain (No Calculator)

a.)
$$8\sin\theta+3=1+6\sin\theta$$
 , $0\leq\theta<2\pi$

b.)
$$\sqrt{3} \sec \theta - 2 = 0$$
, $0^{\circ} \le \theta < 360^{\circ}$

Try:

Solve:

$$\cot \theta + 3 = 2$$
 , $0 \le \theta < 2\pi$

Reminder: When you see a squared trigonometric term, consider using factoring or quadratic equation:

Example 2:

a.)
$$\tan^2 \theta - 4 \tan \theta = 0$$
, $0 \le \theta < 2\pi$

b.)
$$\sin^2 \theta - 3 \sin \theta + 2 = 0, 0^{\circ} \le \theta < 360^{\circ}$$

Try:

$$\cos^2 \theta - \cos \theta - 2 = 0, 0 \le \theta < 2\pi$$

Use a general solution when there is no given range, or if you are asked to use the general solution. The final solution needs to be as simple as possible; you may want to write a few answers to see if a pattern exists.

Example 3: Solve in radians

$$2\cos^2\theta - \cos\theta - 1 = 0$$