

3.4 Equations and Graphs of Polynomial Functions

Without the help of a graphing calculator, a polynomial function can be sketched with the following characteristics:

- a.) Degree
- b.) Sign of leading coefficient
- c.) In a factored form
 - x-intercepts (zeros)
 - multiplicity
- d.) y-intercept

Multiplicity

The **multiplicity** of a function is the number of times a zero is repeated:

Example 1: Determine the zeros and the multiplicities of the corresponding zeros for the function. Then determine the degree.

$$f(x) = (x - 1)^2 (x - 5)(x + 2)^3$$

There are three types of multiplicities at $x = a$

Multiplicity of 1:

The graph passes through the point.

Even multiplicity:

The graph bounces at the point; the higher the multiplicity the wider it appears.

Odd multiplicity:

The graph passes through the point but is similar to a $y = x^3$ graph.

Example 2: Sketch the following:

State the

i.) Degree

ii.) Leading Coefficient

iii.) End behaviours

iv.) zeros

v.) y-intercept

vi.) Regions where the graph is positive

vii.) Regions where the graph is negative

a.) $y = (x - 1)(x + 2)(x + 3)^2$

$$\text{b.) } y = -(2x - 3)^2 (x + 2)^3$$

$$\text{c.) } y = -2x^3 + 6x - 4$$

d.) $y = x^4 - 3x^3 - 6x^2 + 28x - 24$

Example 2: Find a possible equation for the following graphs; determine the least possible degree.

