3.3. Completing the Square

Completing the square is an algebraic process that converts a function from quadratic form to vertex form.

Example 1: Write the following in vertex form:
a.) $f(x)=x^{2}+6 x+5$
b.) $f(x)=3 x^{2}-12 x-9$
c.) $f(x)=-5 x^{2}-70 x$

Try:
a.) $f(x)=x^{2}+8 x-7$
b.) $f(x)=2 x^{2}-20 x$

Example 2: Modeling a real life problem
a.) A farmer has 100 m of fencing available to build an enclosure for his cows. The enclosure only requires 3 sides of fencing, as the $4^{\text {th }}$ side is against the barn. Determine the dimensions of the enclosure that maximizes the area of the enclosure.
b.) A school dance charges $\$ 10$ for an entrance fee for 300 students. They predict that if they decreased the price by $\$ 1$, they would get 10 more students. What is the optimal price to charge?

